



Sonar Implementation Concepts

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Outline

- The sonar environment
- Typical sonar block diagram
- **Brief tour of some topics covered in much greater depth in other courses:**
 - signal representation
 - beamforming
 - signal detection
- Passive processing
- Active processing



References

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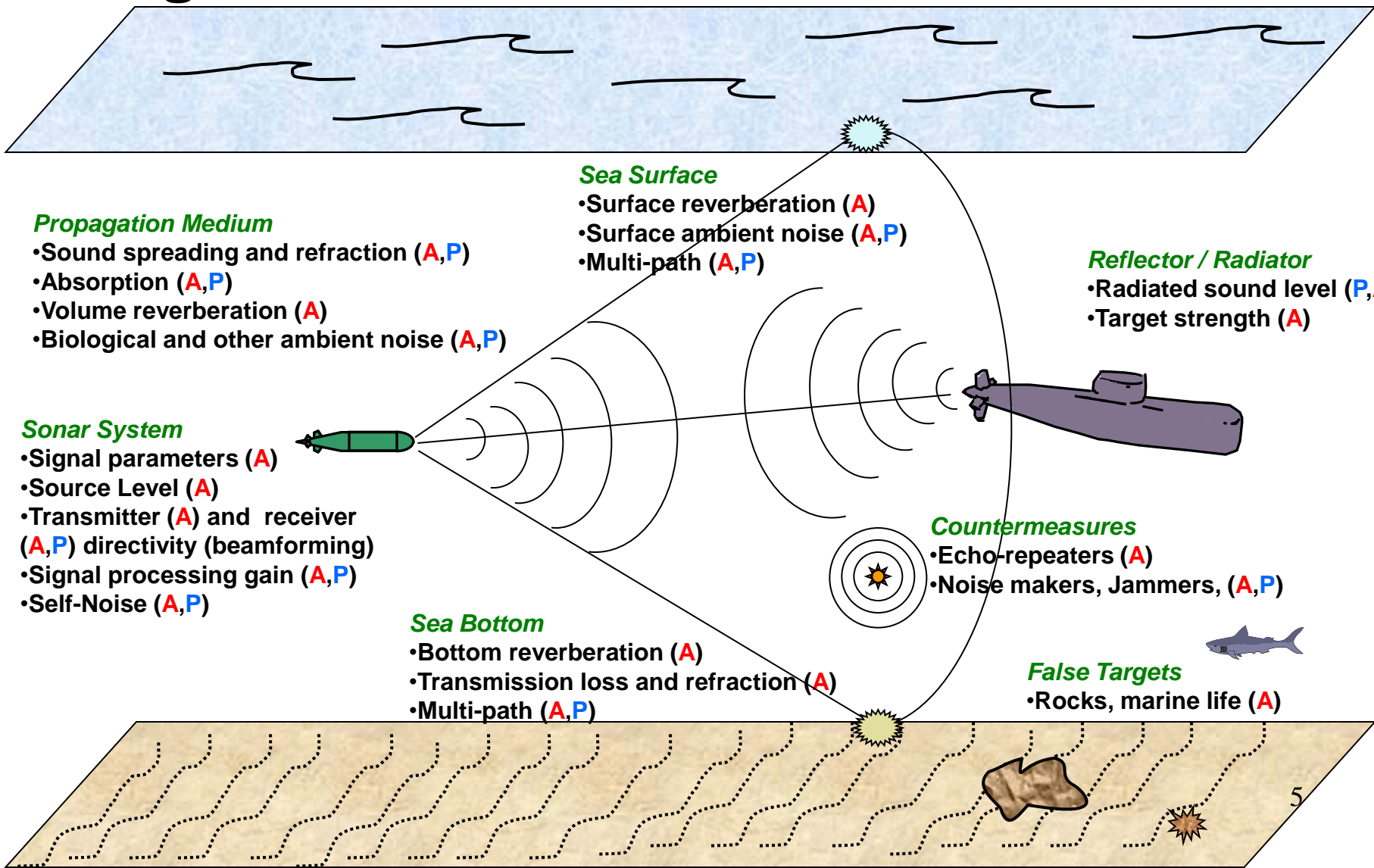
(B) – Basic/Overview/Reference (M) – Mid-level/General/Reference (A) – Advanced/Special Topic



The Sonar Environment and the Sonar Equation



Signals and Noise in Underwater Sonar





The Sonar Equation

- The Sonar Equation represents our confidence about our ability to decide if a signal is present or not.
- Details of the equation are derived using our knowledge of physics, signal processing and statistical decision theory.
- The Sonar Equation, in its simplest form, is:

$$\frac{\text{Signal Power}}{\text{Noise Power}} \begin{matrix} \rangle \\ \langle \end{matrix} \text{Decision Threshold}$$



Decibels

- **Sound power per unit area in an acoustic wave is sound intensity.**
- **For progressive plane waves, sound intensity is proportional to the square of sound pressure.**
- **Sound power is often expressed in decibels, and is always given in relation to some reference. So a signal level (“sound pressure level”), in dB, is related to the signal pressure:**

$$S = 20 * \log_{10}(\text{Signal Pressure/Reference Pressure})$$

- **The reference pressure most often used in underwater acoustics is 1 micro Pascal.**



The Sonar Equation (Cont'd)

- **Signal-to-Noise ratio SNR is sometimes referred to the input to the sonar system (i.e. “in the water”).**
- **The sonar equation is usually expressed in decibels as a difference:**

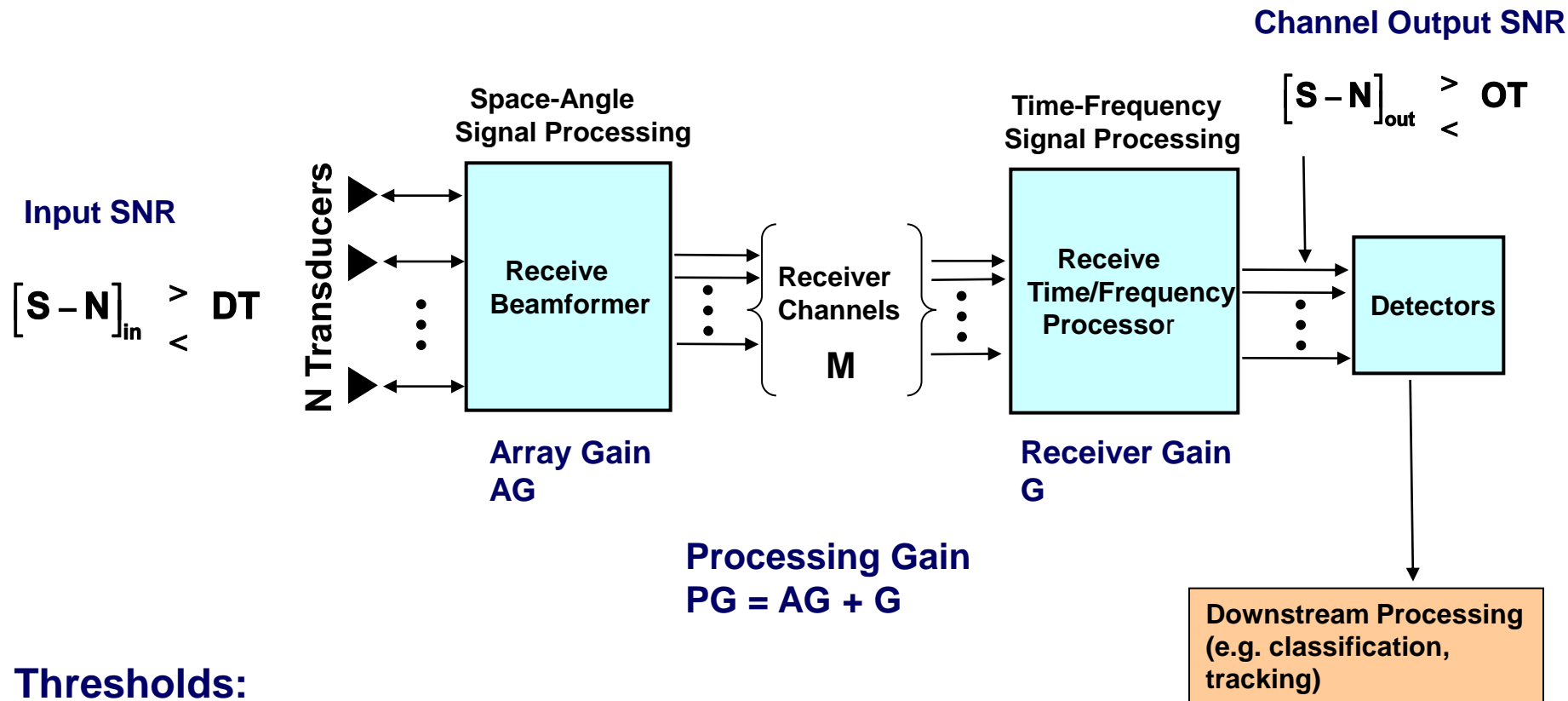
$$[S - N]_{in} - DT \underset{<}{>} 0$$

"Signal Excess"

- **In the above,**
 - **$[S - N]_{in}$ is the signal to noise ratio, expressed in dB, at the input to the sonar system.**
 - **DT is called the input Detection Threshold.**
- **The sonar equation can also be written relative to the receiver output at the point where a detection decision is made.**



Sonar Signal Processing Gain



Thresholds:

- DT = Input Detection Threshold**
- OT = Receiver Output Threshold**
- OT = DT + PG**



Sonar System Gains and Losses

- **An active sonar transmits sound, or a passive source radiates sound, at a given source level.**
- **Sonar equation usually expressed in terms of SNR at some point internal to sonar system (beamformer output or receiver input).**
- **In analyzing the radiated or reflected sound, gains and losses intrinsic to the sonar system must be accounted for:**
- **Losses may include**
 - **Transmit and receive beam pointing errors' effects on signal**
 - **Signal processing losses (“mismatches” of all kinds)**
- **Gains may include**
 - **Beamforming reduction of noise (“array gain”)**
 - **Receiver signal processing gain**



The Sonar Equation (Cont'd)

- **With**

**Receiver Output Threshold (OT) = Input Detection Threshold (DT) +
Sonar Processing Gain (PG)**

- OT depends on desired statistical reliability of receiver and its design characteristics.
 - PG generally depends on the sonar array characteristics, the characteristics of the particular signal being received, and the type of noise that predominates.
- **The Sonar Equation at the receiver output becomes**

where $[S - N]_{\text{out}} - \text{OT} \begin{matrix} > \\ < \end{matrix} 0$

$$[S - N]_{\text{out}} = [S - N]_{\text{in}} + \text{PG}$$



Sonar Equations (Continued)

- **Active Sonar:**

$$S = TL - (20 \cdot \log_{10}(R) + \alpha \cdot R) + TS - (20 \cdot \log_{10}(R) + \alpha \cdot R)$$

$$= TL - (40 \cdot \log_{10}(R) + 2 \cdot \alpha \cdot R) + TS$$

where TL = transmitted level;

TS = target strength;

α = absorption loss coefficient

$$N = 20 \cdot \log_{10}(N_{\text{ambient}} + N_{\text{reverb}} + N_{\text{self}} + N_{\text{target}})$$

- **Passive Sonar:**

$$S = SL - (20 \cdot \log_{10}(R) + \alpha \cdot R)$$

where SL = radiated level of passive source

$$N = 20 \cdot \log_{10}(N_{\text{ambient}} + N_{\text{self}})$$



Signal Sources

- **Active:**

- Received signal is an attenuated and distorted version (echo) of the transmitted signal
- “False targets” and reverberation are echoes of the transmitted signal off of discrete and distributed environmental reflectors

- **Passive**

- Sound radiated from a target can be from machinery, flow noise, target sonar, and other sources



Attenuation

- **Sound is attenuated by spreading and absorption**
 - **Sound spreads out geometrically from its source and again upon reflection**
 - **Absorption in salt water is frequency dependent.**
 - **Higher frequencies suffer greater absorption loss.**
 - **Absorption loss is negligible in fresh water**
- **Active sonar suffers a two-way attenuation loss**



Noise Sources: Ambient

- **Ambient noise is the noise that exists in a particular part of the water irrespective of the presence of the sonar or the target**
- **Sources:**
 - Thermal
 - Biological
 - Noise from the surface: wind, waves, rain
 - Shipping
- **Ambient noise is location, depth, wind speed, and frequency dependent**
- **Simplest ambient noise model is isotropic; real ambient noise is often direction dependent**



Noise Sources: Reverberation

- **Reverberation is the echo of the transmitted signal off of the environment:**
 - boundaries – surface and bottom reverberation
 - scatterers in the water – volume reverberation
- **Reverberation is directly proportional to signal energy and duration.**
- **Reverberation varies as $20 \cdot \log(r) + 2\alpha r$ (volume); $30 \cdot \log(r) + 2\alpha r$ (boundary)**
- **Due to scatterer motion, spectrum of reverberation is spread in relation to signal spectrum**



Noise Sources: Self Noise

- **Self Noise is the noise that the sonar and its vehicle make**
- **Sources:**
 - **Electrical** – usually the lowest noise in the system
 - **Machinery** – may be coherent from channel to channel
 - **Flow through the water** – incoherent from channel to channel
- **Flow noise is usually the dominant source of self noise for a moving sonar system**
- **Flow noise varies as $70 \cdot \log(v/v_{\text{ref}})$ (where v is the sonar platform's velocity and v_{ref} is a reference velocity)**



Noise Sources: Target Radiated Noise

- **Target radiated noise can interfere with active reception. Is often the means of detecting a target passively**
- **Noise varies widely in strength with source type**
- **Noise can have a wide variety of spectral shapes**
- **Noise varies as $20 \cdot \log(r) + \alpha r$**



Target Echo

- The target reflects a replica of the transmitted signal
- The echo level is proportional to the transmitted source level.
- The proportionality “constant” is target strength (TS), a complex measure of the sound reflecting attributes of the target.
- Target echo varies as $40 \cdot \log(r) + 2\alpha r$
- Target echo spectrum of a moving target is doppler shifted relative to transmitted signal



Sonar System Block Diagram

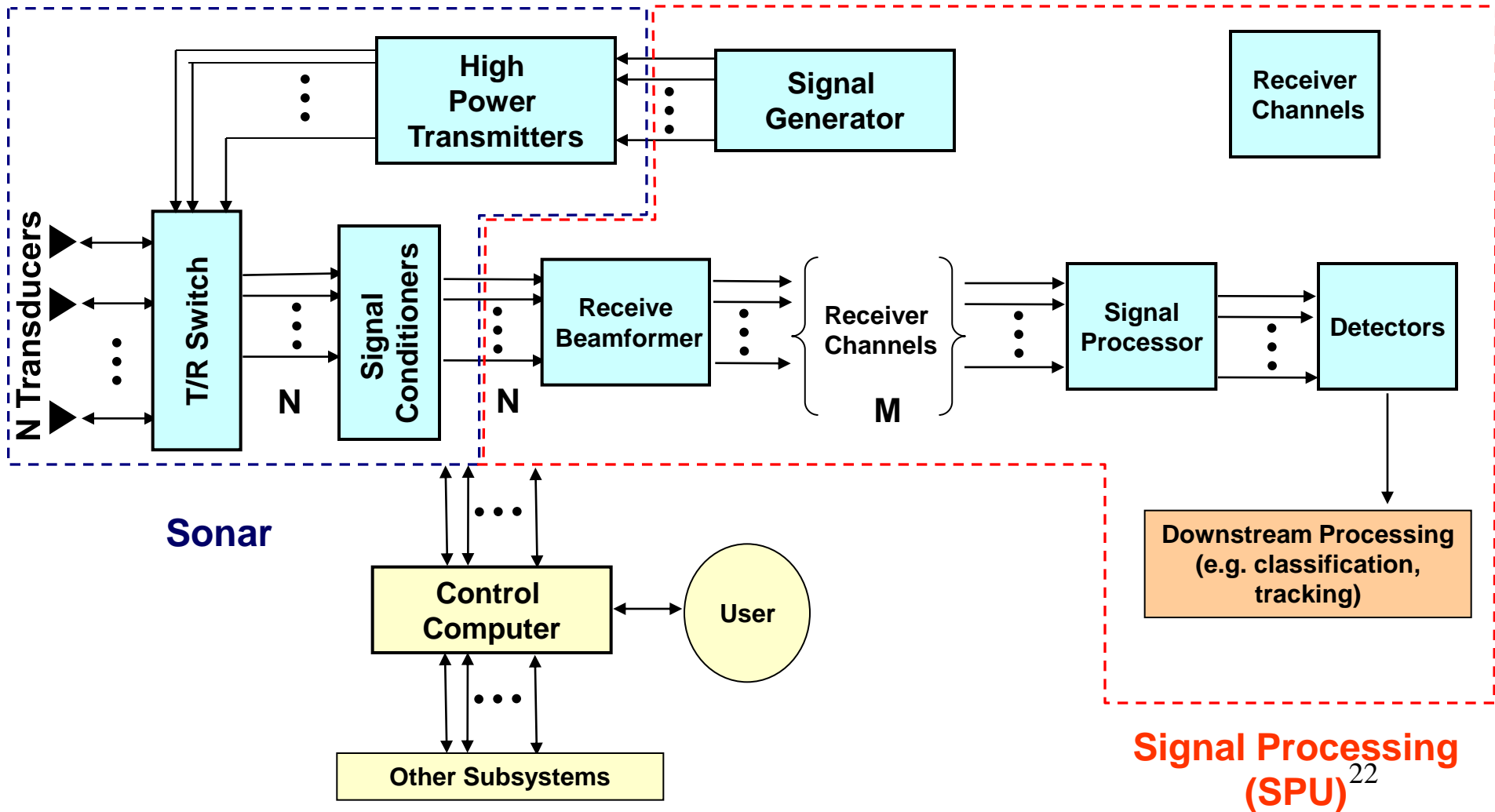


Sonar System

- **A sonar system may be part of a larger system, say an autonomous vehicle, with other subsystems (autopilot, propulsion, etc.)**
- **Sonar systems can contain both a transmitter and receiver, sometimes using the same transducer hardware.**
- **Often broken down into units of the sonar hardware itself, and a signal processing unit (SPU).**



Sonar System Block Diagram





Control Computer

- **Maintains control of all sonar subsystems**
- **Works in concert with other subsystems, e.g. tactical, autopilot, propulsion**
- **Receives and executes commands from the user. These “commands” may be a suite of programmed behaviors for autonomous vehicles.**



Transducers

- **Interface between the ocean and the sonar electronics**
- **Converts sound to electrical impulses and vice-versa**
- **Can be a linear, planar, or volumetric array**
- **Transducer functions:**
 - **Transmit**
 - **Receive**
- **Many transducers perform both functions**



Transducer Transmit Properties

- **Converts electrical signals to acoustic signals**
 - Response given as:
 - pressure at a distance for a given voltage or current drive
 - dB re 1uPa @ 1m re 1 volt. Generally a function of frequency
- **Requirements/Considerations:**
 - High power → low impedance
 - High efficiency
 - Amplitude and phase matched and stable for use in arrays
 - Low 'Q' for wideband operation



Transducer Receive Properties

- **Converts acoustic signals to electrical signals**
 - **Response given as:**
 - voltage out for a given pressure at the transducer
 - dBv re 1uPa. Generally a function of frequency**
- **Requirements/Considerations:**
 - **High sensitivity**
 - **Low noise**
 - **Amplitude and phase matched and stable for use in arrays**
 - **Low 'Q' for wideband operation**



Transmit/Receive (T/R) Switch

- **Connects the transmitter to the transducer for active transmissions**
- **Receiver must be protected from the high transmit power**
- **T/R switch accomplishes this via switching and isolation circuitry**
- **Receiver can still be susceptible to transmitter noise coupling through T/R switch**



Transmit: Signal Generator

- **Provides drive signals to the high power transmitter**
- **Controls:**
 - **Signal waveform generation**
 - amplitude
 - phase (frequency)
 - **Multiple transmit sequencing**
 - **Transmit beam shaping**
 - **Transmit beam steering**
 - **Own-Doppler nullification (ODN)**



Transmit: High Power Transmitters

- **Converts low level input signals to high power drive signals**
 - Input from the signal generator
 - Output drives the transducer elements
- **Considerations:**
 - High power output
 - High efficiency
 - Variable load impedance when used in arrays



Receive: Signal Conditioners

- **Peak signal limiting**
- **Impedance matching**
- **Pre-amplification**
- **Band pass filtering**



Receive Beamformer

- **Combines conditioned transducer signals to form beams**
- **Each beam acts as a spatial filter**
- **Uses beam shading and beam steering to form beam sets**
- **Each receive beam processed in its own channel**
- **Typical beam types:**
 - **Multiple narrow detection beams**
 - **Sum-difference beams**
 - **Offset phase center beams**



Receiver Channels

- **Each receive beam has a receiver channel**
- **Receiver channel functions:**
 - **Band pass filtering**
 - **Gain control (historic progression in order of sophistication)**
 - **Fixed gain**
 - **Time varying gain**
 - **Automatic gain control**
 - **Detection processing within the angular space that defines that channel**



Receive: Signal Processor

- **Processes beam signals to enhance their signal to noise ratio (SNR)**
- **Matched filter processing**
 - **Active**
 - **Passive**
- **Performs target angle calculations**



Receive: Detectors

- **Applies a threshold to the signal processor output signals**
- **Fixed threshold:**
 - **Constant probability of detection (CPOD)**
- **Variable threshold:**
 - **Constant false alarm rate (CFAR)**
 - **Requires background estimation**

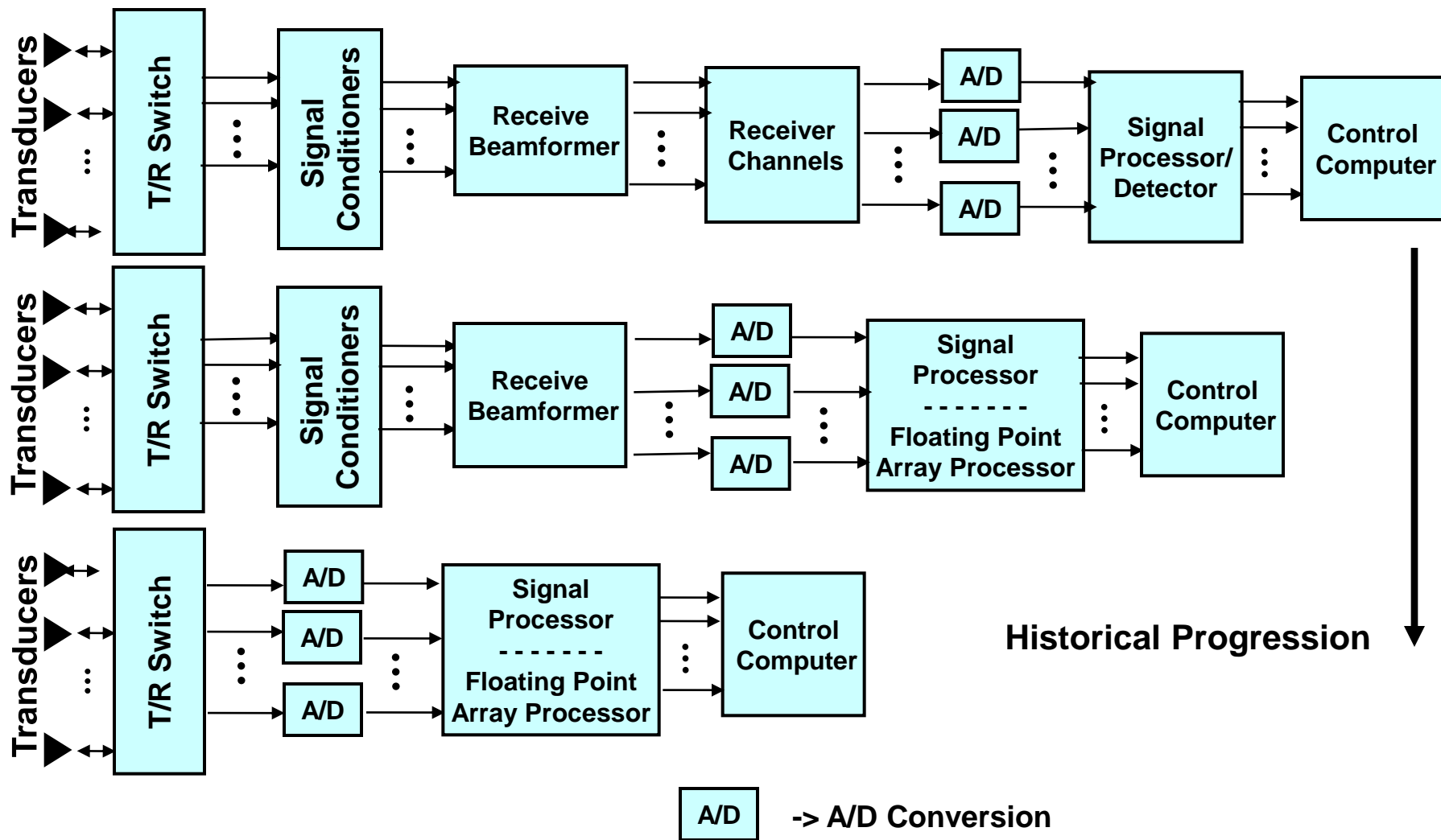


Digital Receiver Goals

- **Stable performance**
- **Flexible design**
- **Smaller size**
- **Lower cost**
- **Historical progression:**
 - **Replace analog receiver circuits with digital signal processor**



Digital Receiver Configurations





Digital Receiver Design Considerations

- **Operating Frequency**
 - Plays into beamwidth, coverage, absorption loss, detection range
- **Receiver bandwidth**
 - Trend today is wideband signals and receivers
- **Dynamic range**
 - Instantaneous (Size of A/D)
 - Long term (Gain adjustment over mission).
- **Out-of-band signals**



Downstream From Detectors

(Beyond Scope of This Course)

- **Clustering – Can the signal that passed the threshold be associated with detections from other channels?**
- **Classification – Does the clustered object have the characteristics of the type of target we are interested in?**
- **Data Fusion – Can the object be associated with a similar object from another sensor?**
- **Tracking – Does the object persist in time? Can we estimate its motion?**



Signal Representation



What Is A Signal?

- **A signal is a change or disturbance in the normal “background” environment that conveys information**
- **The disturbance can be electrical, optical, mechanical, acoustical, etc.**
- **The information is contained in the way the disturbance changes**
 - with time
 - with frequency
 - in space
 - in direction
- **Acoustical signals are disturbances in the background pressure level in the medium (air, water, etc.)**



Real and Complex Signals

- A real-valued function of time, $f(t)$, or space, $f(x)$, or both, $f(x,t)$, is often called a “real signal”.
- It is sometimes useful for purposes of analysis to represent a signal as a complex valued function of space, time, or both:

$$s(t) = u(t) + i \cdot v(t)$$

- More often, such a function is written in polar form:

$$s(t) = R(t) \cdot e^{i\phi(t)}$$

where

$$R(t) = \sqrt{u^2(t) + v^2(t)} \quad (\text{magnitude})$$

$$\phi(t) = \arctan\left(\frac{v(t)}{u(t)}\right) \quad (\text{phase})$$

- The real-world signal $f(t)$ represented by $s(t)$ is just the real part of $s(t)$:

$$f(t) = \Re\{s(t)\} = u(t) = R(t)\cos(\phi(t))$$



What Is Signal Processing?

- **Signal processing is altering the properties of a signal to achieve some effect. In sonar, signal processing generally done to enhance the signal-to-noise ratio in order increase the probability of detection of a target, or to continue detecting a target.**
- **Signal processing can be done on the temporally or spatially varying signal, or on its *spectrum* (see the following).**
- **Most modern signal processing is done digitally. A time signal is sampled and converted to a set of numbers using an analog-to-digital (A/D) converter. Signal processing is then done by mathematical operations on the set of numbers.**



Spectral (Fourier) Analysis

- Any signal, real or complex, that varies with time can be “broken up into its spectrum” in a way similar to that in which light breaks up into its constituent colors by a prism
- The mathematical operation by which this is accomplished is the *Fourier transform*
- The Fourier transform of a time signal yields the “frequency content” of a signal
- Much signal processing is done in the “frequency domain” by means of mathematical operations (filters) on the Fourier transforms of the signals of interest
- The result of the processing can be converted back to a filtered time signal by means of the *inverse Fourier transform*



Frequency Domain Signal Processing

- **Frequency domain signal processing, or “filtering” alters the frequency spectrum of a time signal to achieve a desired result.**
- **Examples of filters: band pass, band stop, low pass, high pass, “coloring”,**
- **Analog filters are electrical devices that work directly on the time signal and shape its spectrum electronically.**
- **Most filtering nowadays is done digitally. The spectrum of a sampled, digitized time signal is calculated using the Fast Fourier Transform (FFT). The FFT is a sampled version of the signal’s spectrum. Mathematical operations are performed on the sampled spectrum.**
- **Samples of the filtered signal are recovered using the inverse FFT.**



Beamforming



What Is Beamforming?

- **Beamforming is spatial filtering, a means of transmitting or receiving sound preferentially in some directions over others.**
- **Beamforming is exactly analogous to frequency domain analysis of time signals.**
- **In time/frequency filtering, the frequency content of a time signal is revealed by its Fourier transform.**
- **In beamforming, the angular (directional) spectrum of a signal is revealed by Fourier analysis of the way sound excites different parts of the set of transducers.**
- **Beamforming can be accomplished physically (shaping and moving a transducer), electrically (analog delay circuitry), or mathematically (digital signal processing).**

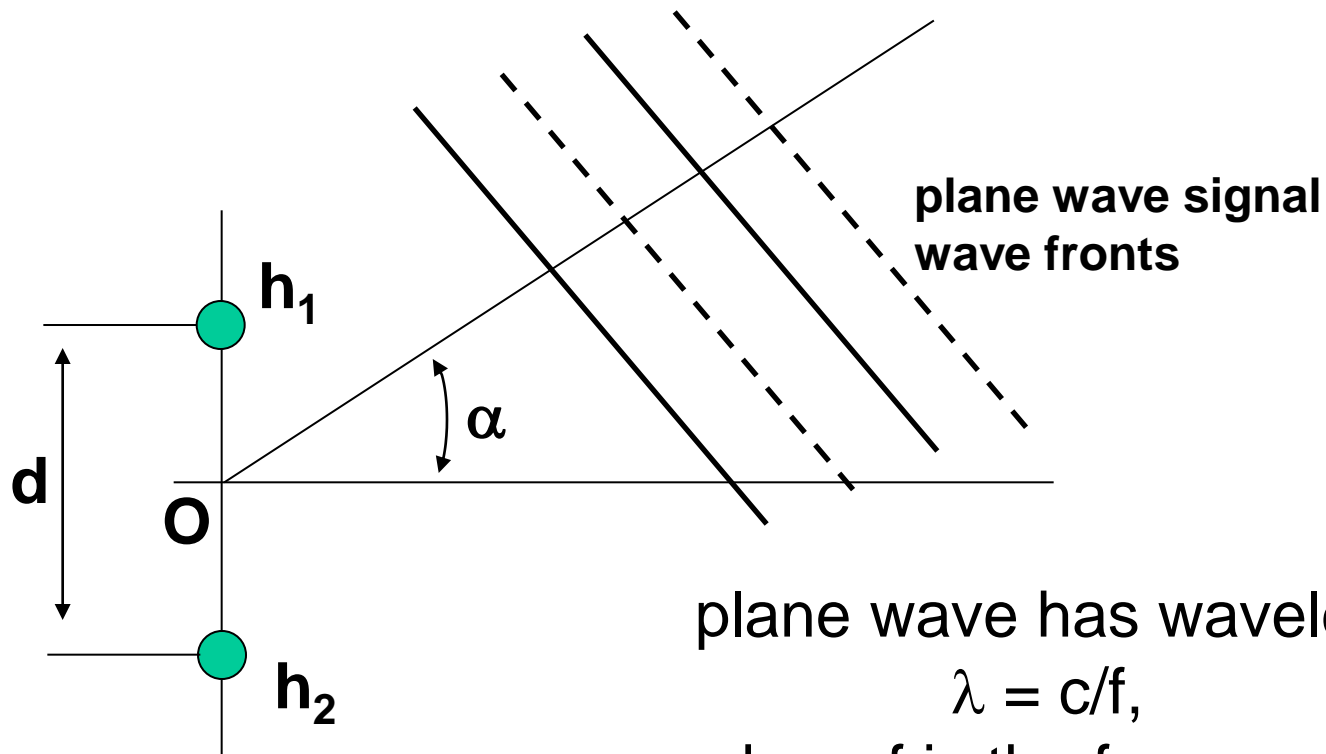


Beamforming Requirements

- **Directivity** – A beamformer is a spatial filter and can be used to increase the signal-to-noise ratio by blocking most of the noise outside the directions of interest.
- **Side lobe control** – No filter is ideal. Must balance main lobe directivity and side lobe levels, which are related.
- **Beam steering** – A beamformer can be electronically steered, with some degradation in performance.
- **Beamformer pattern function is frequency dependent:**
 - Main lobe narrows with increasing frequency
 - For beamformers made of discrete hydrophones, spatial aliasing (“grating lobes”) can occur when the the hydrophones are spaced a wavelength or greater apart.



A Simple Beamformer



h_1 h_2 are two omnidirectional hydrophones spaced a distance d apart about the origin O

plane wave has wavelength $\lambda = c/f$,
 where f is the frequency
 c is the speed of sound



Analysis of Simple Beamformer

- Given a signal incident at the center O of the array:

$$\mathbf{s}(t) = R(t) \cdot e^{i\omega(t)}$$

- Then the signals at the two hydrophones are:

$$\mathbf{s}_i(t) = R(t) \cdot e^{i\omega(t)} e^{i\phi_i(t)}$$

where

$$\phi_n = (-1)^n \frac{\pi d}{\lambda} \sin \alpha$$

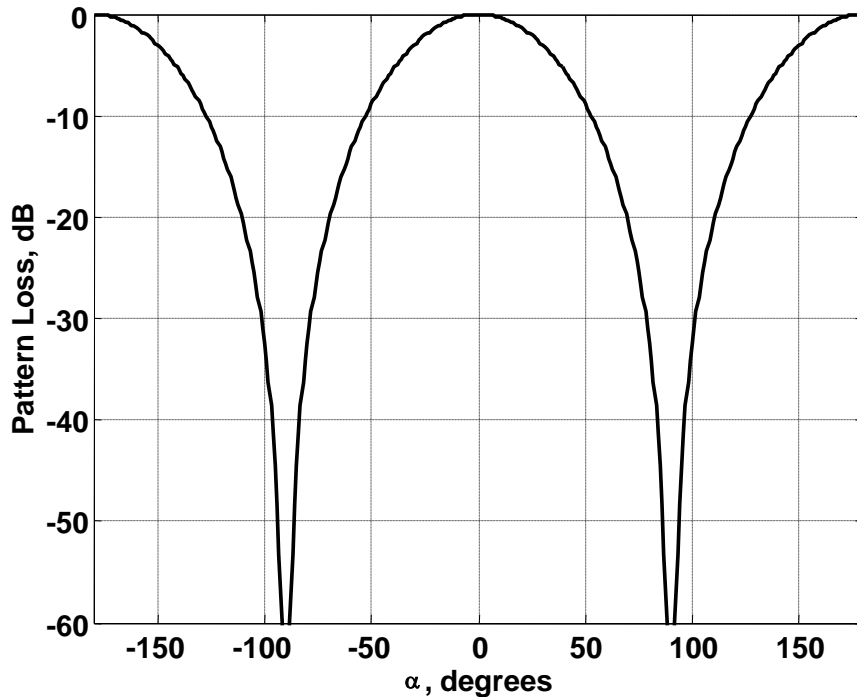
- The pattern function of the dipole is the normalized response of the dipole as a function of angle:

$$b(\alpha) = \frac{\mathbf{s}_1 + \mathbf{s}_2}{\mathbf{s}} = \cos\left(\frac{\pi d}{\lambda} \sin \alpha\right)$$

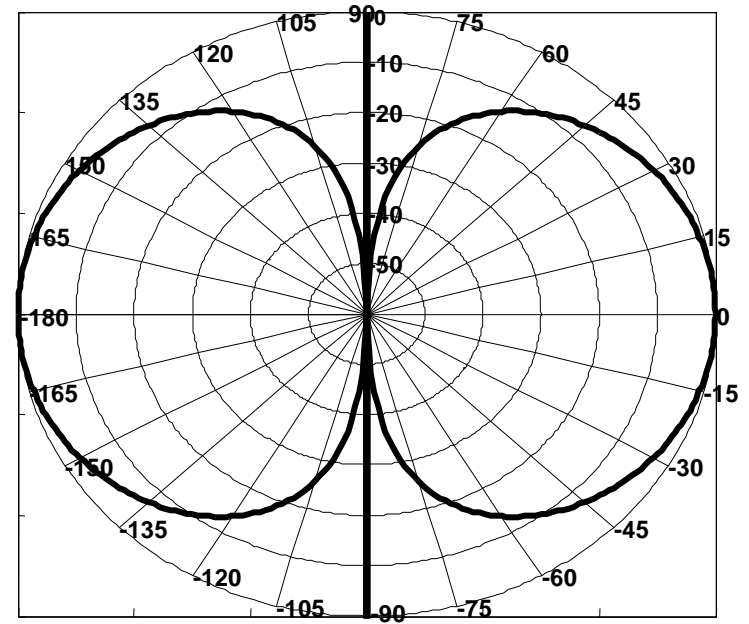


Beam Pattern of Simple Beamformer

Pattern Loss vs. Angle of Incidence of Plane Wave For Two Element Beamformer, $\lambda/2$ Element Spacing



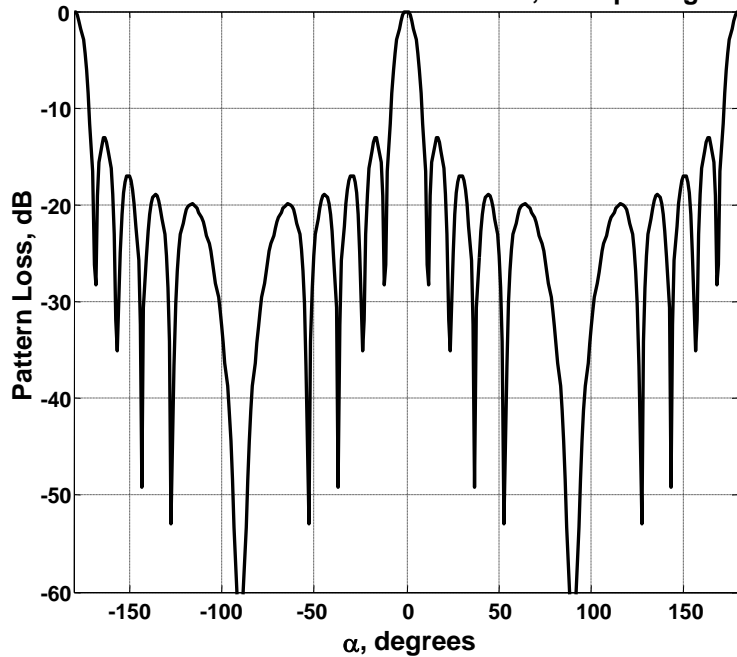
Polar Plot of Pattern Loss For 2 Element Beamformer $\lambda/2$ Element Spacing



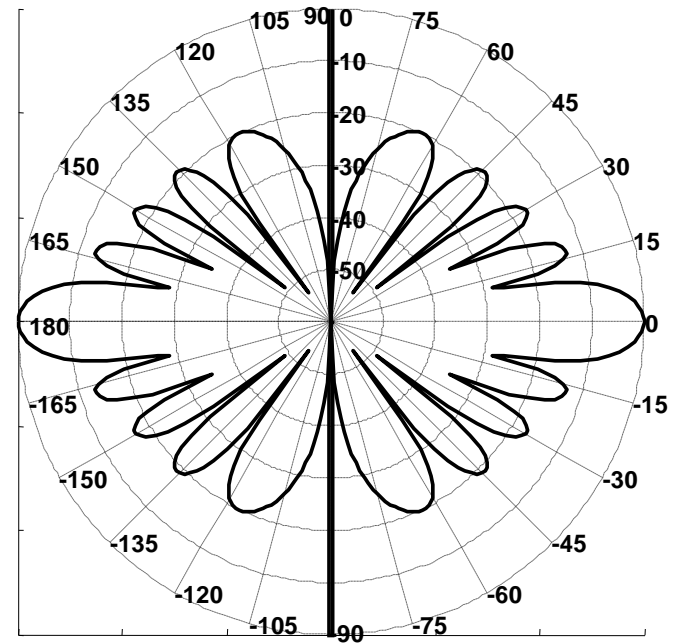


Beam Pattern of a 10 Element Array

Pattern Loss vs. Angle of Incidence of Plane Wave
For Ten Element Beamformer, $\lambda/2$ Spacing



Polar Plot of Pattern Loss For 10 Element Beamformer
 $\lambda/2$ Spacing





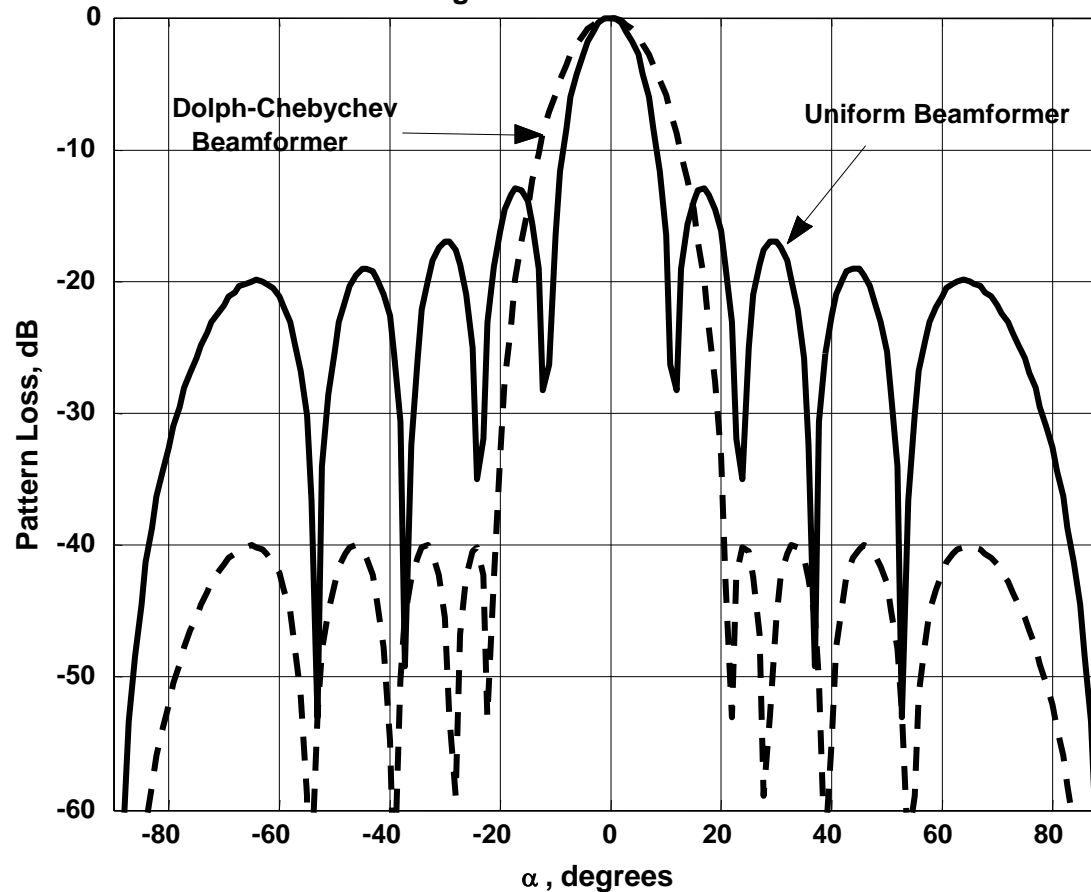
Beamforming – Amplitude Shading

- **Amplitude shading is applied as a beamforming function, usually to the received signal.**
- **Each hydrophone signal is multiplied by a “shading weight”**
- **Effect on beam pattern:**
 - **Used to reduce side lobes**
 - **Results in main lobe broadening**



Beam Pattern of a 10 Element Dolph-Chebyshev Shaded Array

Comparison Beam Pattern Of A 10 Element Dolph-Chebyshev Beamformer With -40 dB Side Lobes And $\lambda/2$ Element Spacing With A Uniformly Weighted 10 Element Beamformer





Beamforming – Receive Beam Steering

- **To electronically steer a beam to a specific angle, the hydrophone signals must add so that a plane wave received at the desired angle would add in-phase.**
- **Beam steering implementations:**
 - Time delay
 - Phase shift



Beamforming – Transmit

- **High power**
 - Transmit the maximum power on each hydrophone
 - Maximum power limited by cavitation
- **Desire broad beamwidth for search, narrow beamwidth for homing**
 - Desire maximum output power for both types of transmits -> Generally do not use amplitude shading on transmit
 - Transmit beamforming accomplished by phase shading of transmit hydrophones



Signal Detection

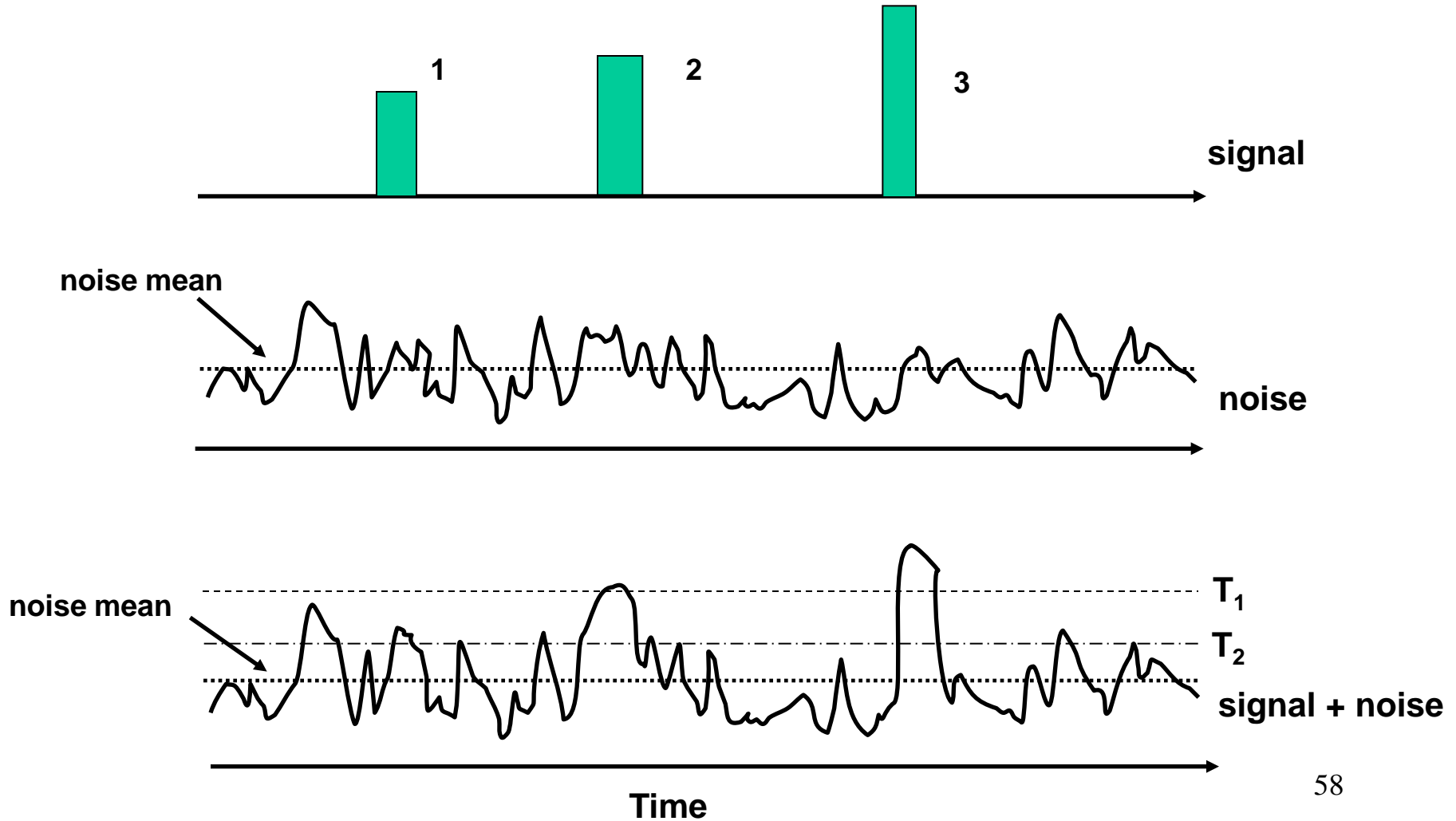


Signal Detection

- **Input to detector is signal plus noise.**
- **Requirements expressed in terms of**
 - probability of detection
 - probability of false alarm
- **Threshold for declaring detection is set based on models for signal and noise**
- **Noise background estimation can be performed on data to improve model.**
- **Outputs of detector are threshold crossings**
- **Performance defined by receiver operating characteristic (ROC) curve – probability of detection vs. probability of false alarm for a particular SNR.**



Detection In Noise



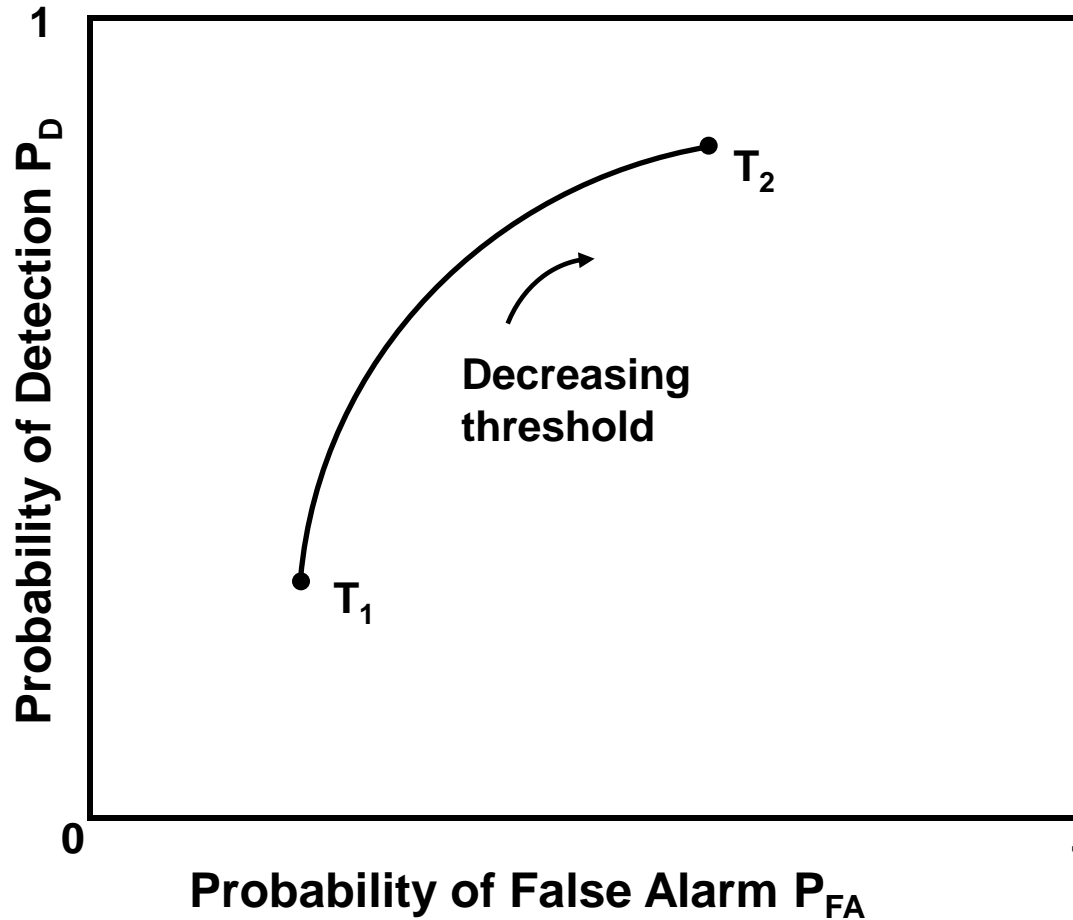


Detection Threshold

- **Performance Criteria:**
 - Probability of detection P_D
 - Probability of false alarm P_{FA}
- **These criteria are not independent: a lower threshold increases P_D , but also increases P_{FA} .**
- **Theoretical ROC is used to set thresholds.**
- **True test is performance in water.**



Receiver Operating Curve (ROC)





Noise Background Estimation

- **A moving average of the received signal is calculated. This average is used to estimate the background noise level.**
- **Against noise that changes rapidly with time – e.g. reverberation, noise level must be continually re-estimated for the entire listening interval. -> Use moving average.**
- **Care must be taken not to average over desired echo, but still get a useful average. Window is usually taken to be the length of the transmitted pulse.**
- **Higher order statistics can also be estimated this way.**



Passive Processing



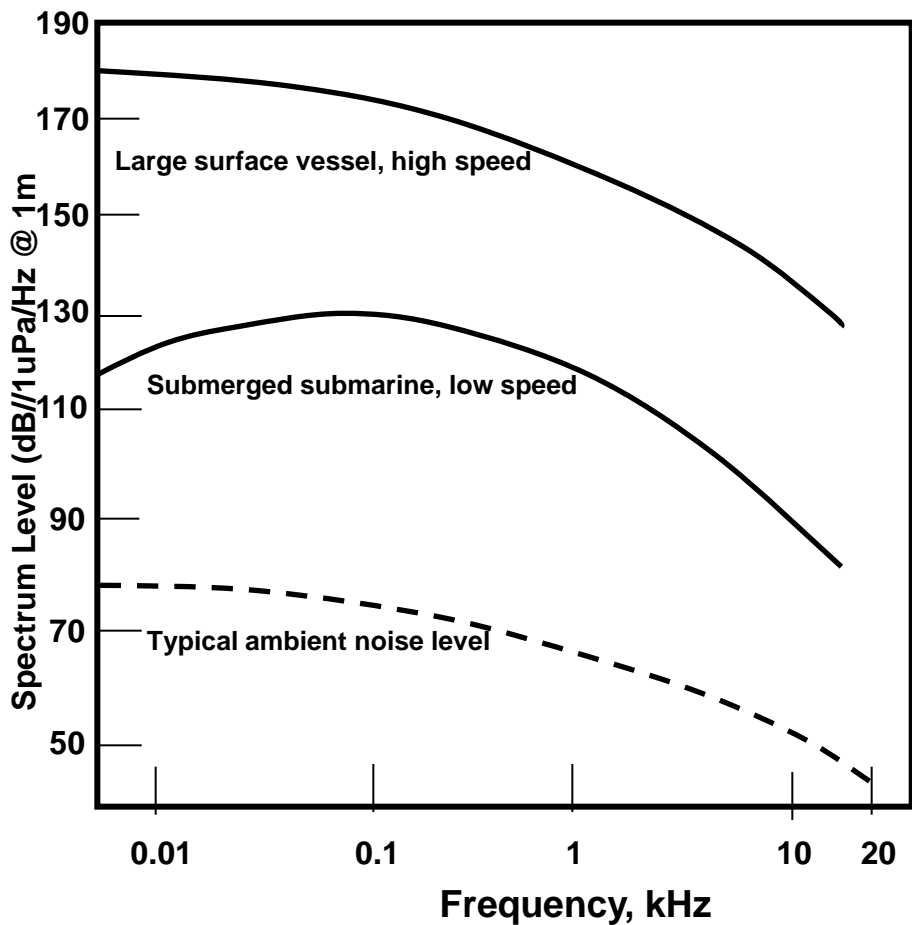
Passive Processing Requirements

- **Targets:**
 - Surface ships
 - Submarines
 - Other sources, e.g. pipeline leaks
- **Target Characteristics:**
 - Broad band
 - Level and spectrum dependent on target speed
 - Narrow band
 - Spectral lines
 - Propulsion system
 - Propeller cavitation
 - Auxiliary machinery
 - Spatially compact

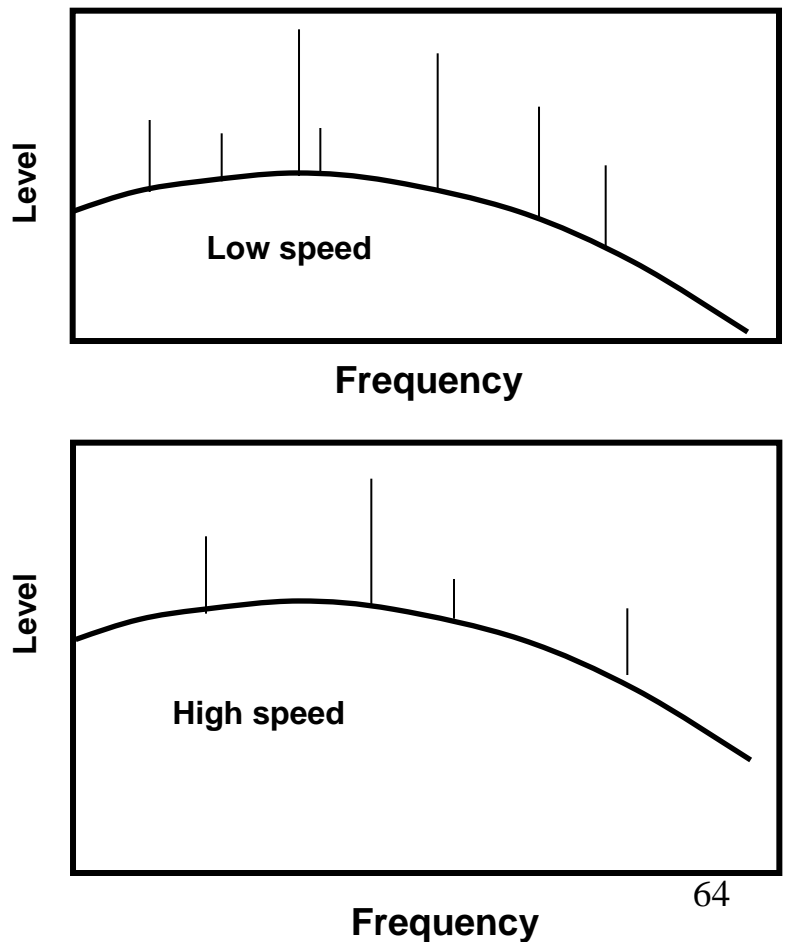


Target Emissions

Some Typical Spectrum Levels For Surface Ships and Submarines



Broadband and Narrowband Components Of a Submarine Signature at Low and High Speeds





Passive Sonar Requirements

- **Target Detection**
 - Passive sonar has an advantage over active for detection range - less spreading and absorption loss.
- **Target Localization**
 - Angle to target
 - Precise localization, especially in range and velocity, is more difficult with passive sonar
- **Target Characterization**
 - Target signatures help identify target
 - Passive sonar won't mistake a rock for a target
 - Active is much more useful for discerning size, shape and structural features



Passive Sonar Capabilities

- **Beamforming**
 - Spatial filter
 - Increased signal-to-noise – directivity
 - Reduces unwanted (out of beam) signals
- **Receiver**
 - Bandpass filter – reduces out of band signals and noise
 - Gain adjust – adjust to receiver circuitry, does not increase SNR
- **Signal processor**
- **Detector**



Passive Multibeam

- **Increases detection capabilities**
 - Wide angle coverage
 - Directivity of individual beams increase SNR
 - Detection processing
 - Beam power comparison among beams
- **Localization**
 - Provides bearing to target to within beam resolution
- **Target identification if spectral processing is used.**



Passive Narrowband Signal Processing

- **FFT (Spectral Processing)**
 - Used to detect tones
 - Improves detection
 - Aids localization by estimating Doppler using frequency changes in the signal
- **Can identify target if its signature is known**



Passive Short Baseline Localization

- **Useful for small sonar arrays**
- **Technique – offset phase center beams**
 - **Uses the correlation between the inputs of two subarrays of a beamformer to estimate the angle to the target.**
 - **The subarrays are closely spaced – $3/2 \lambda$ or $1/2 \lambda$ are often used.**
 - **Useful for enhancing passive detection performance by allowing fine estimate of angle to detection.**



Passive Long Baseline Localization

- **Useful for arrays of widely spaced hydrophones**
- **Technique – Correlation processing with variable time shift**
 - **Time shift with highest correlation gives time delay for reception between each hydrophone.**
 - **Useful for enhancing passive detection performance.**
 - **Can be used to estimate angle to target. Multiple hydrophones (3 or more) can be used to triangulate.**



Active Processing



Active Sonar Requirements

- **Target Detection**
- **Target Localization**
 - **Range**
 - **Angle**
 - **Doppler -> line-of-sight velocity**
- **Target Characterization**
 - **Size**
 - **Shape**
 - **Orientation**
 - **Finer details**

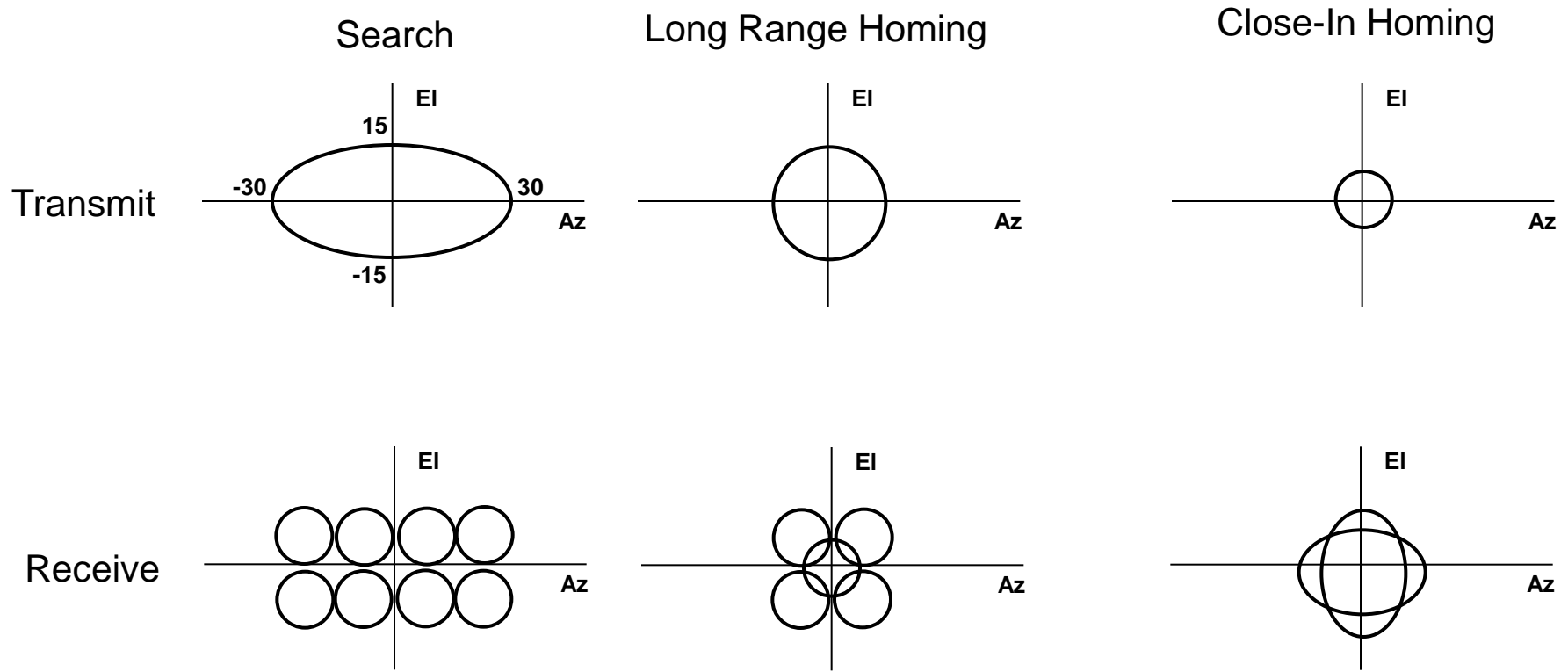


Typical Active Beamformer Configurations

- **Transmit**
 - **Wide angle – search volume coverage**
 - **Narrow angle – homing**
 - **Source level increases as beam narrows**
- **Receive**
 - **Search – Multiple narrow beams for high directivity**
 - **Homing – Narrow detection beam with offset phase beams**



Active Sonar Beamsets



3 dB Beamformer Contours

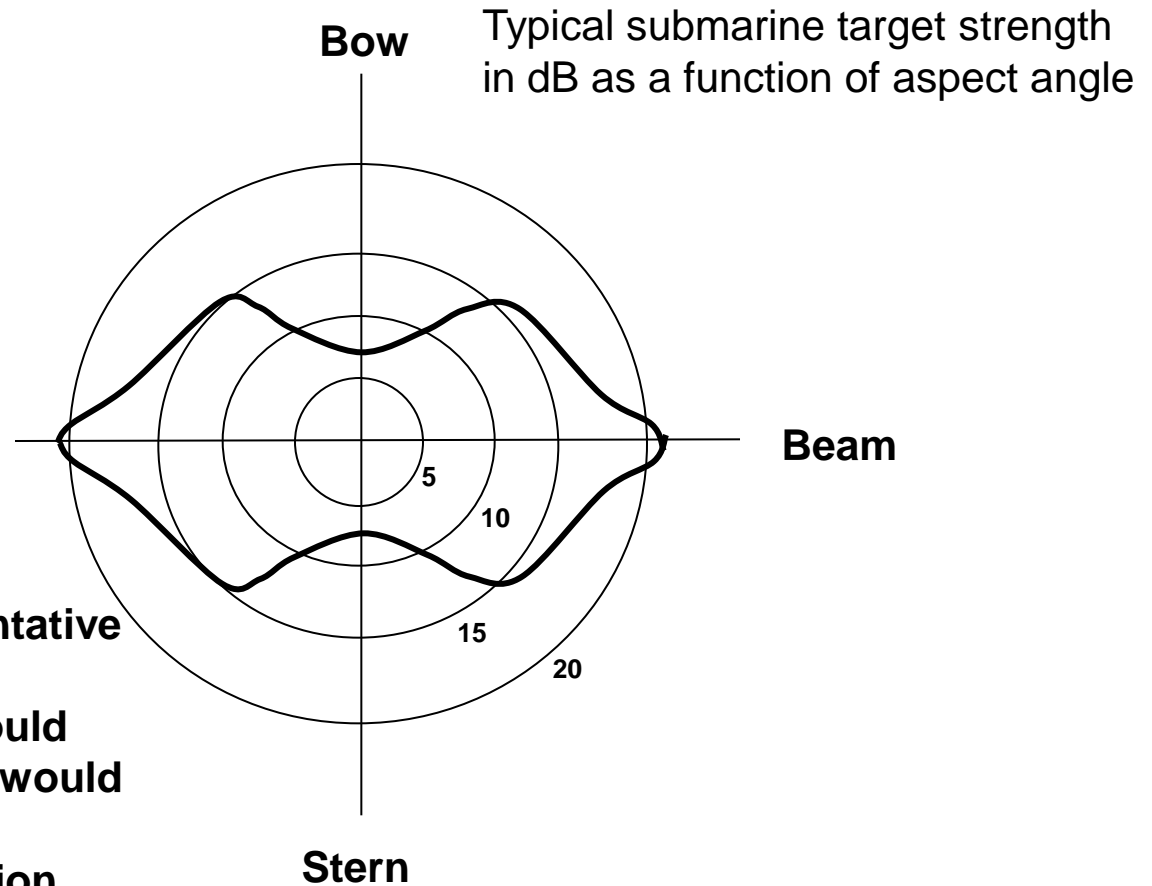


Target Properties

- **After accounting for propagation losses, the target echo level is proportional to the transmitted source level**
- **The proportionality “constant” is the *target strength***
 - **Depends on sound reflecting properties of the target**
 - **Function of frequency, signal resolution, and aspect angle**
 - **Target highlights (echoes from reflecting surfaces) add with random phase.**



Variation of Target Strength



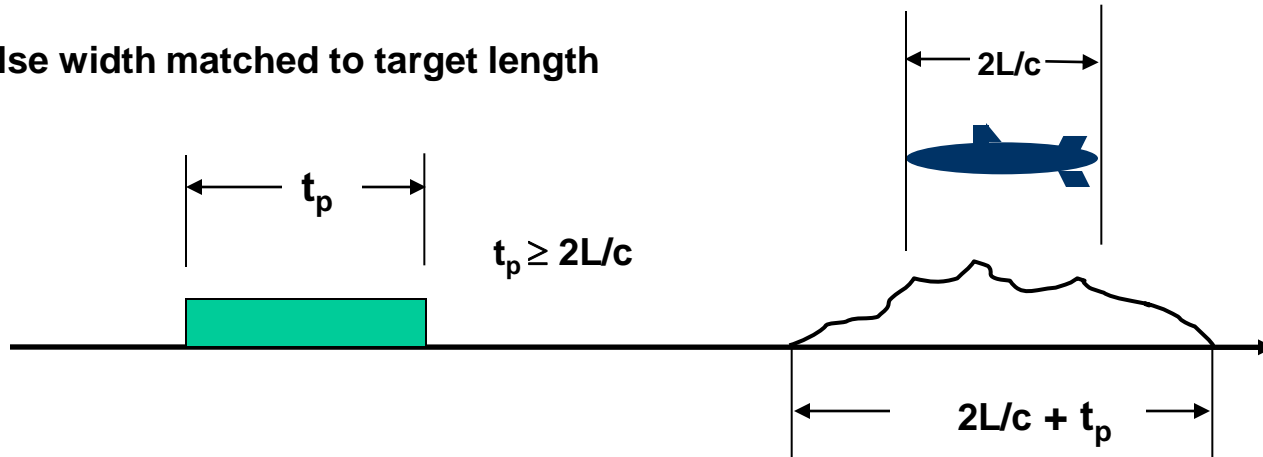
Notes:

- TS is a function of frequency
- Graph at right is more representative of a low frequency
- High frequency graph of TS would have similar rough shape, but would have significantly more detail
- “Spikier” due to higher resolution of target features

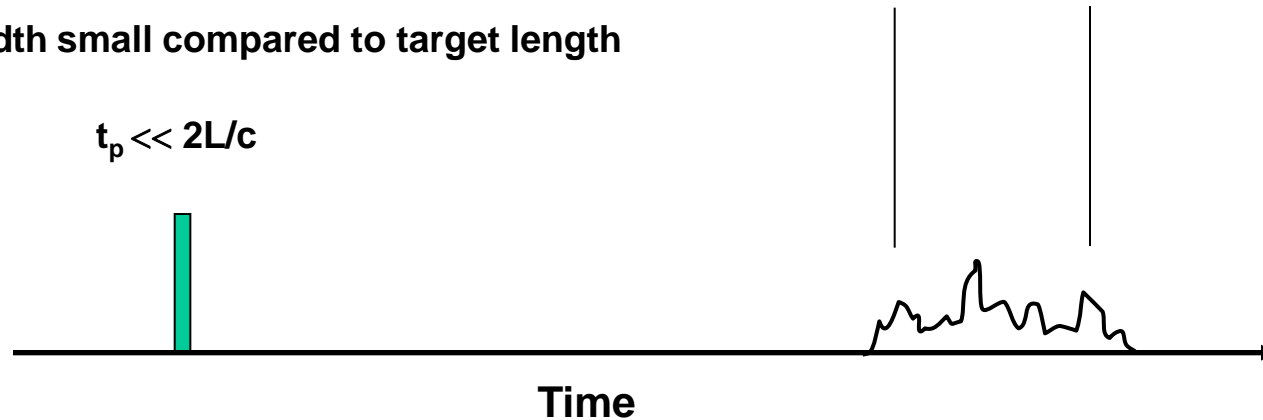


Target Echo and Signal Resolution

Pulse width matched to target length



Pulse width small compared to target length





Effect of Motion on Echo

- **For stationary sonar and target:**
 - Echo spectrum \approx Signal spectrum
- **For moving sonar or target, spectrum of echo is shifted and spread.**
- **Shift is “Doppler shift”. Doppler shift is due to:**
 - Target motion
 - Sonar motion
- **Doppler shift due to sonar motion can be somewhat negated by shifting the transmit or receive frequency to account for sonar motion – own-Doppler nullification (ODN).**
- **Spectral spreading is due to numerous factors, in particular the fact that different parts of the target move with different speeds relative to line-of-sight vector.**



Effect of Reverberation

- **For stationary conditions (“quiet sea”):**
 - Reverberation spectrum \approx Signal spectrum
- **Spectrum of reverberation is more generally shifted and spread.**
- **Spectral shift and spreading is due to:**
 - **Scatterer motion**
 - Surface reverb scatterer motion dependent on sea state
 - Volume reverb scatterer motion depends, e.g., on presence of fish, suspended bubbles or solid material, currents, etc.
 - **Sonar motion**
 - Off-axis scattering

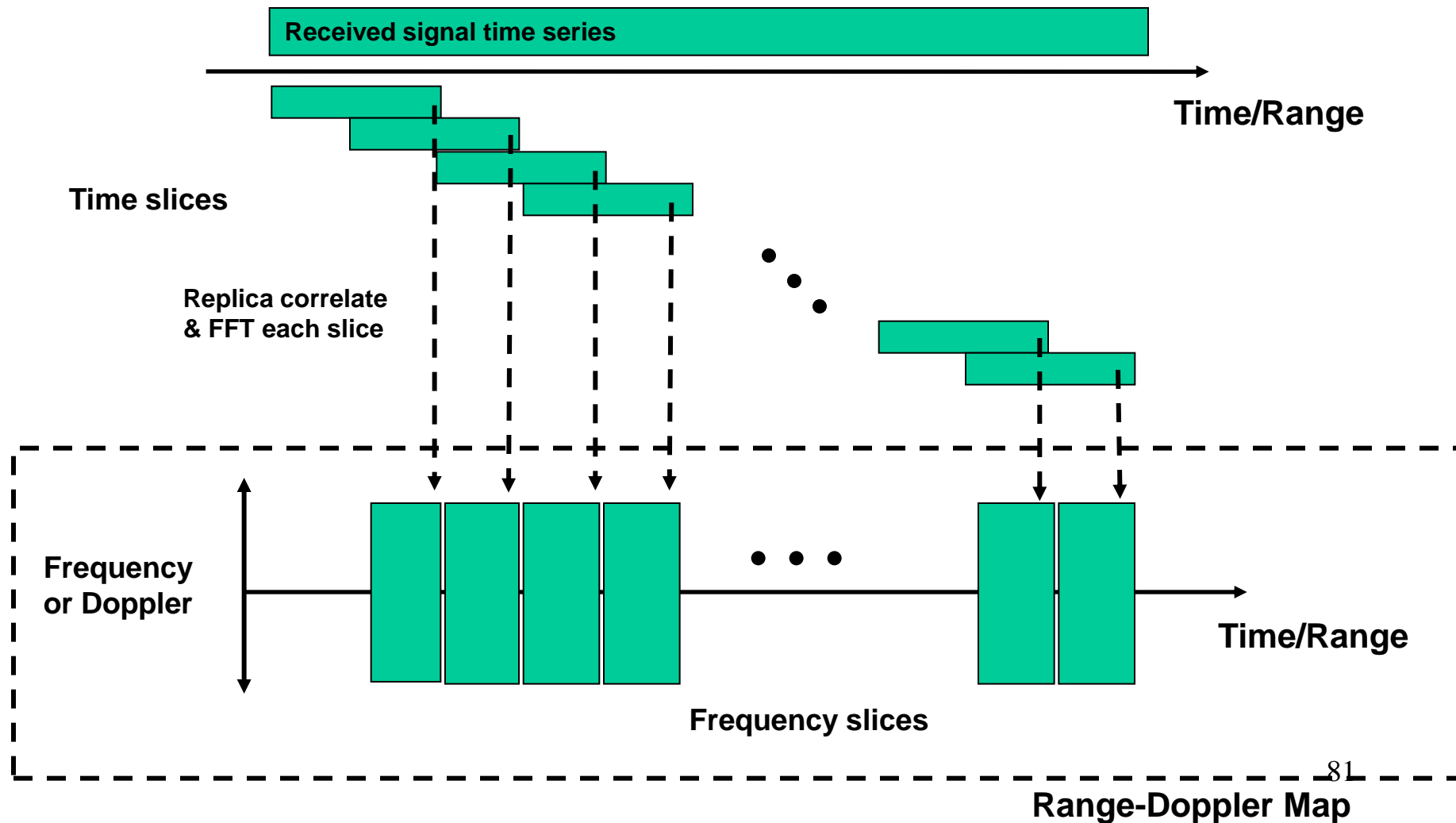


Active Detection Processing

- **One of the most common active detectors is the matched filter.**
 - **Peak output SNR is optimized against additive white Gaussian noise with a matched filter.**
- **Can be implemented by correlating received signal with replica of transmitted signal at varying time shifts.**
 - **Time shift with peak output above threshold yields target range,**
- **To account for frequency (Doppler) shift in received signal due to target motion, the detector is usually implemented in the frequency domain – frequency shifted detections can be located on “Range-Doppler map.**



Matched Filter Implementation





Range-Doppler Maps

- **A Range-Doppler map is a representation of the power spectral level of an acoustic echo as a function of time.**
- **The time axis is usually converted to range, while the frequency axis is converted to equivalent Doppler shift.**
- **The resulting surface is reduced to a two dimensional plot for presentation using colors to represent level.**
- **The levels in each Range-Doppler cell can be processed to find detections.**



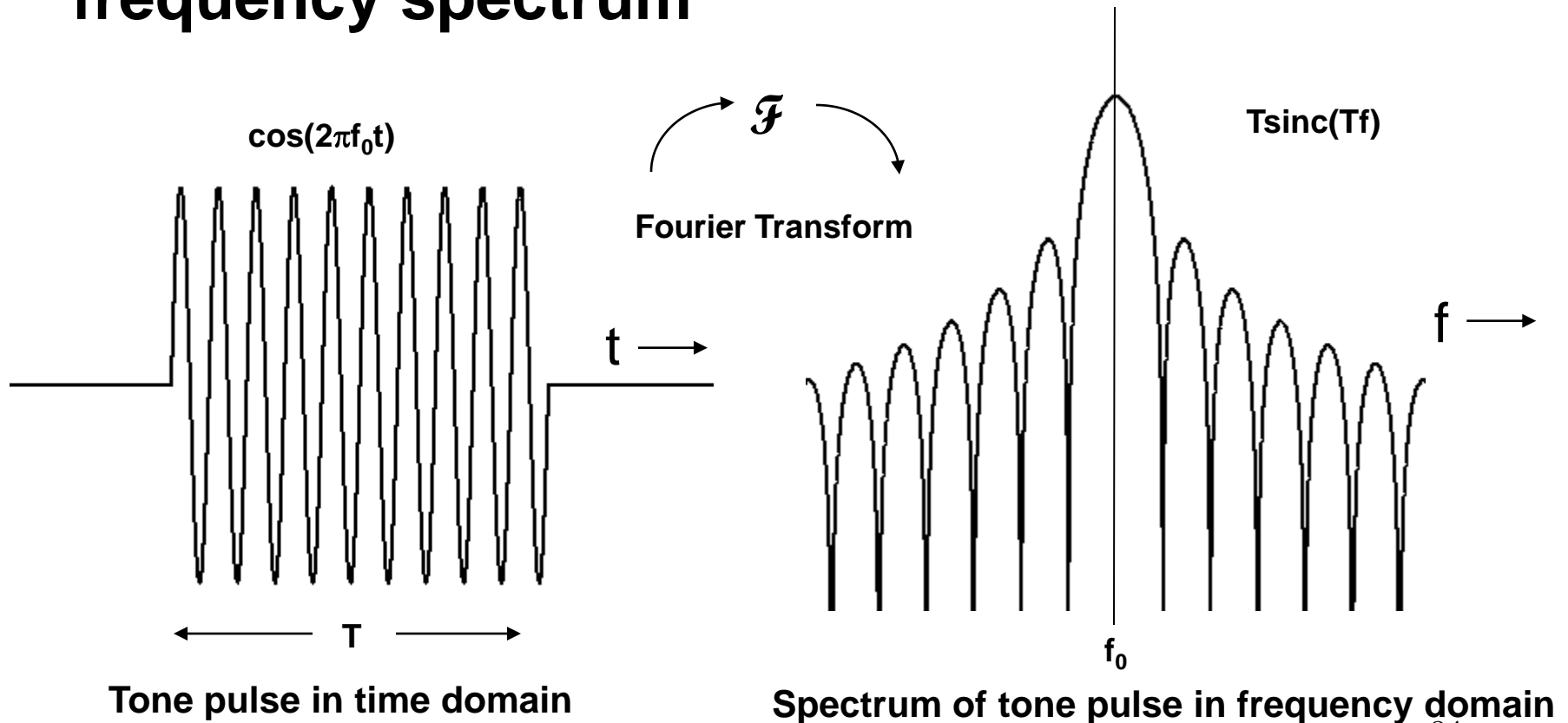
Effect of Reverberation (Continued)

- Reverberation is an echo of the transmitted signal.
- When ODN is used, the reverberation spectrum is centered at about the transmit frequency (zero frequency when basebanded).
- The spectrum continues as long as the reverberation can be detected. (“Reverb ridge”)
- Even though target echo level falls off faster than reverberation with range, targets off of the reverb ridge (high Doppler targets) can be detected at long range.
- Signal design for low Doppler targets attempts to mitigate effects of reverb ridge.



Example of Range Doppler Map

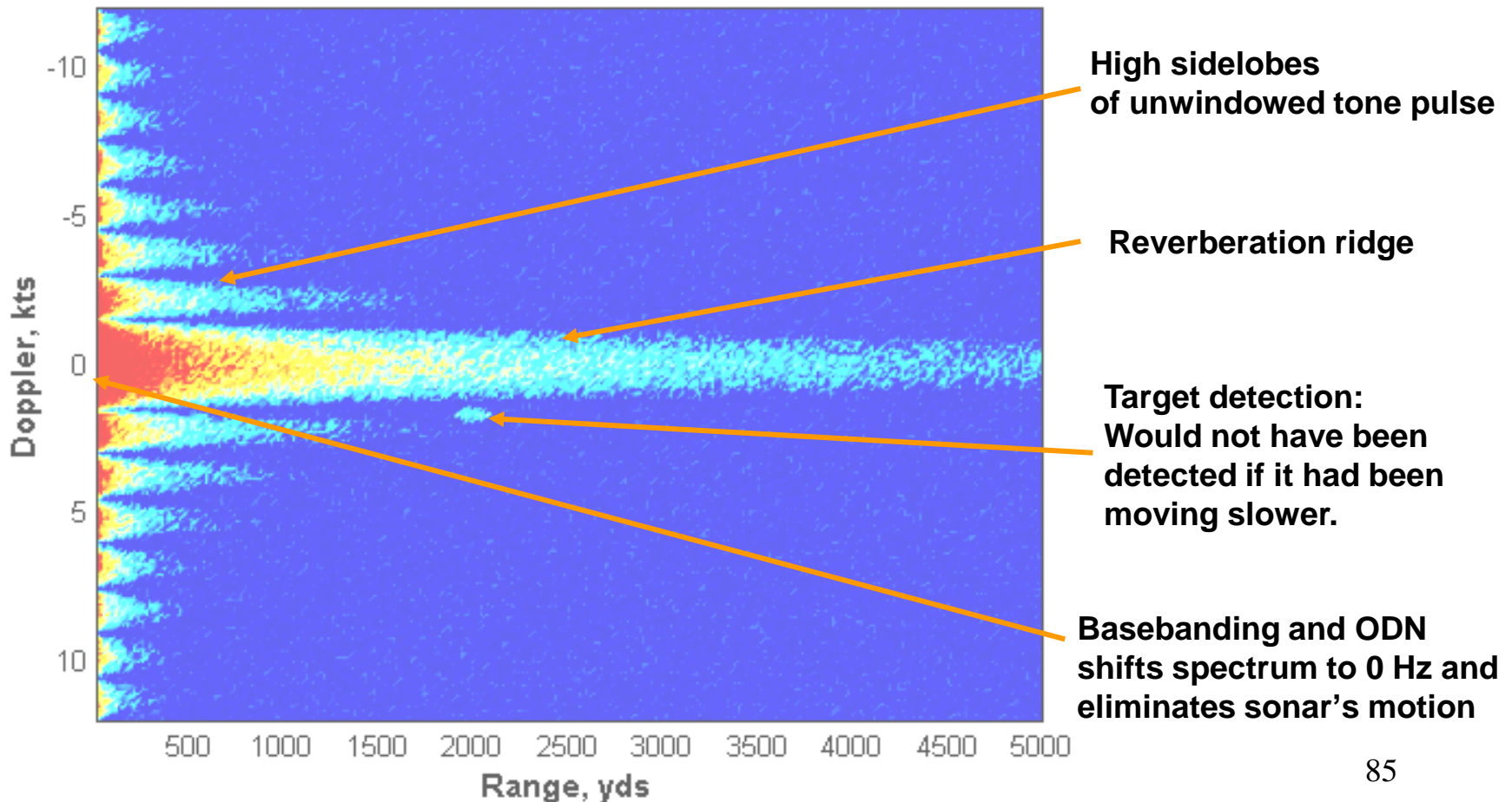
- Unwindowed tone pulse has sinc-function frequency spectrum





Example Of A Range-Doppler Map (Volume Reverberation, Stationary Sonar)

Example Range Doppler Map





Signal Selection

- **Range resolution is inversely proportional to signal bandwidth.**
 - For tone pulses, this translates to range resolution is proportional to pulse length:
 - Pulse bandwidth is inversely proportional to tone pulse duration, so
 - Short pulses => Short (“high”) range resolution
 - For linear FM sweeps, range resolution is inversely proportional to width of sweep.
 - Wide frequency sweep => Short (“high”) range resolution
- **Doppler resolution is inversely proportional to pulse length.**
 - Short pulse duration => Wide (“low”) Doppler resolution



High Doppler Targets

- **Tone pulses can be good choices for high Doppler targets:**
 - Target is out of the reverberation ridge
 - Longer pulses used for detection have excellent Doppler resolution
 - Short pulses used for close-in homing have excellent range resolution.
- **Drawbacks:**
 - Targets that are changing aspect can be lost in reverberation ridge
 - As sonar closes in on target, short pulses are used. Reverberation spectrum is very wide for short pulses. Can lose even high Doppler targets



Low Doppler Targets

- **Processing gains can be attained against low Doppler targets by using linear sweep FM pulses.**
- **Advantages: spreads (and hence lowers) reverberation power over bandwidth of frequency sweep, but coherently processes echo => Processing gain $\sim 10 \cdot \log(TW)$, where T is pulse length and W is signal bandwidth**
- **Drawbacks:**
 - **Increasing T to increase PG is not viable when target is very close or target position is changing rapidly. But short T means less Doppler resolution.**