

For each of the conics:

- Identify class/type, b. write in standard form, and c. indicate position, that is center/vertex and "Which way does it open?" or "Which direction does the major axis or the transverse axis lie?"
- Provide your answers in the appropriate box. Thank you.

1. $x^2 + x + 2y - \frac{3}{4} = 0$

Class/type:

parabola

Standard Equation:

$$(x + \frac{1}{2})^2 = -2(y - \frac{1}{2})$$

Center/Vertex

Direction:

vertex $(-\frac{1}{2}, \frac{1}{2})$
opens down

2. $4y^2 + 9x^2 + 18x - 27 = 0$

Class/type:

ellipse

Standard Equation:

$$\frac{y^2}{9} + \frac{(x+1)^2}{4} = 1$$

Center/Vertex

Direction:

center $(-1, 0)$
vertical major axis

3. $25x^2 - 4y^2 + 50x + 16y - 91 = 0$

Class/type:

hyperbola

Standard Equation:

$$\frac{(x+1)^2}{4} - \frac{(y-2)^2}{25} = 1$$

Center/Vertex

Direction:

center $(-1, 2)$
horizontal transverse axis
opens left and right

$$x^2 + x + 2y - \frac{3}{4} = 0$$

$$x^2 + x = -2y + \frac{3}{4}$$

$$x^2 + x + \frac{1}{4} = -2y + \frac{3}{4} + \frac{1}{4}$$

$$(x + \frac{1}{2})^2 = -2y + 1$$

$$(x + \frac{1}{2})^2 = -2(y - \frac{1}{2})$$

opens down vertex $(-\frac{1}{2}, \frac{1}{2})$

$$4y^2 + 9x^2 + 18x - 27 = 0$$

$$4y^2 + 9x^2 + 18x = 27$$

$$4y^2 + 9(x^2 + 2x) = 27$$

$$4y^2 + 9(x^2 + 2x + 1) = 27 + 9$$

$$4y^2 + 9(x+1)^2 = 36$$

$$\frac{y^2}{9} + \frac{(x+1)^2}{4} = 1$$

center $(-1, 0)$ major axis vertical

$$25x^2 - 4y^2 + 50x + 16y - 91 = 0$$

$$25x^2 + 50x - 4y^2 + 16y = 91$$

$$25(x^2 + 2x) - 4(y^2 - 4y) = 91$$

$$25(x^2 + 2x + 1) - 4(y^2 - 4y + 4) = 91 + 25 - 16$$

$$25(x+1)^2 - 4(y-2)^2 = 100$$

$$\frac{(x+1)^2}{4} - \frac{(y-2)^2}{25} = 1$$

center $(-1, 2)$ transverse axis

horizontal

opens left and right